

Formal Verification of a Fail-Safe Cross-Chain Bridge

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Abstract

Cross-chain bridges are financial services that interconnect blockchains. High monetary values flow through these bridges, and their security must be safeguarded. However, designing real-world cross-chain bridges is a difficult endeavor. Due to blockchain's closed-world nature, tokens cannot be transferred from a sender to a receiver chain; on the contrary, they need complex logic that maintains an equilibrium on both chains, even if either the chains or the bridge fail. This paper formally verifies a model of a novel fail-safe cross-chain bridge to ensure correctness. We define formal requirements and prove the bridge is safe using the Isabelle/HOL proof assistant.

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1 Introduction

The blockchain ecosystem has rapidly evolved over the last decade, most notably with the rise of Ethereum [33] and Bitcoin [24]. At the end of 2024, the top 636 smart contract blockchains had a market cap of 2.9 trillion dollars [12].

As the blockchain ecosystem continues to grow, it has become increasingly heterogeneous, consisting of blockchains with unique designs and varying characteristics (proof-of-work, proof-of-stake, costs, performance, programming languages, etc.). Thus, each blockchain provides users with a diverse experience, security guarantees, and financial incentives, making it unlikely that a single dominant blockchain design will emerge [8].

Unfortunately, without a method of communication between blockchains, the advantages of a multichain world are limited. Since blockchains have *closed-world assumption* about their tokens, digital assets are not universal entities and cannot exist outside of their chains.

To this end, decentralized cross-chain bridges have been proposed (e.g., [34]) to provide interoperability between blockchains. Given two blockchains, a cross-chain bridge allows users to transfer tokens from a *sender chain* C_s to a *receiver chain* C_r . When an asset is transferred from C_s to C_r , the asset is *locked* on C_s , and a new asset is *minted* on C_r , representing the original asset on C_s . When the newly created asset is transferred back to chain C_s , the corresponding asset on C_r is *burned*, and the locked asset on C_s is *released*. Smart contracts on both blockchains implement this protocol, and a *relay network* is used to establish communication between the two chains.

Given the various security exploits targeting bridges [19, 20, 35], designing a safe bridge is paramount. Developing a safe bridge involves guaranteeing several *safety and liquidity invariants*. For instance, we want to ensure that there is always a 1-to-1 relationship between locked and minted assets. Otherwise, double-spending [18] attacks may arise. Liquidity invariants guarantee that the user can always perform an action to access their asset. The



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bridge has *fail safety*, i.e., that all tokens will be unlocked in a blockchain C_s if blockchain C_r irrecoverably crashes.

Standard audit and testing methods can be employed to increase the likelihood of safety on the bridge. However, these methods, due to their inability to account for all possible behaviors, are insufficient. This is evidenced by the fact that bridges have become notorious targets for hackers. As of 2024, bridge-related hacks cost more than \$2.8 billion, representing approximately 40% of all hacks in the Web3 [17]. Given the potential for sizable losses, relying only on ad-hoc testing and auditing techniques is perilous. A more rigorous method to ensure bridge safety is to employ *formal verification*. Here, we construct mathematical objects describing the bridge behavior and mathematical proofs to ensure the bridge protocol is correct for all possible inputs and configurations.

This paper presents an industrial case study in which we formally prove the safety of the formal abstract model of SONIC GATEWAY. This cross-chain bridge provides interoperability between the Ethereum and SONIC blockchains. While formal methods have been employed for individual blockchain components [6], to the best of our knowledge, our work is the first to prove the safety of a fail-safe cross-chain bridge model formally.

We formalize the bridge within the interactive theorem prover Isabelle/HOL [26] and establish safety by identifying and proving several fundamental safety properties. We perform our verification using a *stepwise refinement approach* [32, 10]: We start with an abstract model and then refine it by adding more and more implementation details. This process has verified the final SONIC GATEWAY design and contributed to the design of cross-chain bridges by identifying essential properties that are pervasive to all fail-safe cross-chain bridges.

Our contributions are summarized as follows:

1. A detailed formal description of the fail-safe SONIC GATEWAY cross-chain bridge including safety properties,
2. A formal specification and correctness proof for the SONIC GATEWAY cross-chain bridge,
3. Experimental evaluation and experience of the verification effort.

This paper is structured as follows. Section 2 describes the SONIC GATEWAY bridge. In Section 3, we detail the formal specification of the SONIC GATEWAY bridge, and in Section 4, we provide a corresponding proof of its safety. We evaluate the verification process in Section 5, and Section 6 details related work. We conclude in Section 7.

2 The Fail Safe Bridge

This section describes the SONIC GATEWAY fail-safe cross-chain bridge. A detailed example of bridge operations is given in Appendix A. The bridge is illustrated in Figure 1. Here, the bridge operates on a pair of blockchains C_s and C_r , where C_s is the sender chain, used to deposit (aka. lock) tokens, and C_r is the receiver chain, used to claim (aka. mint) tokens. The blockchain C_s has a smart contract $SC_{deposit}$, and C_r has a smart contract SC_{claim} . For simplicity, we assume that users transfer fungible tokens from an ERC20 [30] contract T_{orig} (although these could also be native tokens of C_s) to C_r , where they are represented by tokens on a dedicated ERC20 contract T_{mint} .

2.1 Token Exchange

During normal bridge operations, users can exchange original tokens on C_s for minted tokens on C_r . At any time, the minted tokens can be converted back to the original tokens in C_s . Token transfers from C_s to C_r operate using a pair of transactions denoted as *Lock* and

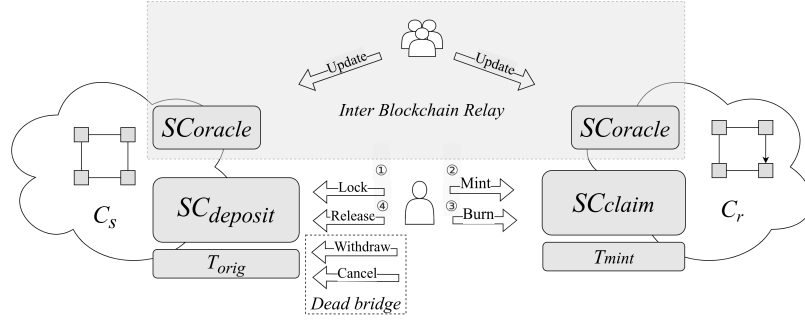
89 *Mint*. Assuming that a user already has at least $v T_{orig}$ tokens available on C_s , the user
 90 invokes a *Lock* transaction on C_s (step ①) to transfer $v T_{orig}$ tokens from their balance
 91 to the $SC_{deposit}$ balance. To verify that a *Lock* transaction has been successfully executed,
 92 $SC_{deposit}$ keeps a log *locks*, containing data about all executed lock transactions (a unique
 93 transaction ID is mapped to data about the caller, token, and amount, usually combined
 94 into a hash value). Before $v T_{mint}$ tokens can be issued by SC_{claim} on C_r (using a *Mint*,
 95 step ②), the solvency needs to be ensured. SC_{claim} issues new tokens only if the user has
 96 locked tokens on $SC_{deposit}$. This requires SC_{claim} (operating on C_r) to read the state of
 97 $SC_{deposit}$ from a different blockchain (C_s), which it cannot do directly. To enable this, the
 98 bridge uses a Merkle proof (a path of a Merkle tree [16]), which acts as a trusted witness for
 99 blockchain C_r of the existence of a specific transaction (or its effect) at a block height t on
 100 blockchain C_s . This Merkle proof is an argument for the *Mint* transaction. Simultaneously,
 101 the state root hash of the world state of C_s is shipped via the trusted channel, which we
 102 call the *Inter-Blockchain Communication (IBC) Relay*. We assume that a special contract
 103 SC_{oracle} keeps track of state root hashes and that a consensus of trusted users regularly
 104 updates it by invoking *Update* transactions. When executing a *Mint* transaction, the contract
 105 SC_{claim} on C_r verifies that the *Lock* transaction took place on C_s at block height t using the
 106 Merkle proof and state root hash of C_s read from SC_{oracle} , which confirm that the log *locks*
 107 contains valid data about the *Lock* transaction. If the proof verification succeeds, the user's
 108 balance of T_{mint} is increased by v (v tokens are minted "out of thin air"). To prevent double
 109 claims of the same deposit, SC_{claim} keeps a directory *mints* of minted deposits. Once the
 110 user obtains T_{mint} tokens on C_r , they can trade with them as with all other ERC20 tokens.

111 At any point, a user with T_{mint} tokens on C_r can exchange them for the same amount
 112 of T_{orig} on C_s . This is done by performing a sequence of *Burn* and *Release* operations,
 113 which are pretty similar to *Lock* and *Mint*, so we do not describe them in detail. The user
 114 invokes a *Burn* transaction (step ③), which removes v tokens from their balance on T_{mint} ,
 115 and the information about this is logged in the *burns* log on SC_{claim} on C_r . After SC_{oracle}
 116 has been informed about the root of the world state of C_r , the user can invoke a *Release*
 117 transaction (step ④) in C_s that contains a Merkle tree proof confirming that the *Burn*
 118 transaction has been successfully executed. Once the proof verification succeeds, $v T_{orig}$
 119 tokens are transferred from the $SC_{deposit}$ balance to the user's one.

120 2.2 Fail-Safety

121 What is unique to the SONIC GATEWAY is that it implements a mechanism that enables
 122 users to retrieve their funds on C_s , even if the bridge goes out of operation (if SC_{claim} or
 123 T_{mint} contracts or even the C_r blockchain stop operating). The bridge is declared dead
 124 once the SC_{oracle} contract (on C_s) does not execute a state root update transaction within
 125 a fixed amount of time (e.g., 7 days). The bridge is declared dead by setting a *dead* flag
 126 in the $SC_{deposit}$ contract and by copying the last known state root of C_r from SC_{oracle} to
 127 $SC_{deposit}$. Once the bridge is declared dead, this status cannot be undone. When the bridge
 128 is dead, users retrieve their assets using *Withdraw* and *Cancel* transactions. Furthermore,
 129 note that *Release* transactions do not depend on C_r and are executed similarly, regardless of
 130 whether the bridge is dead.

131 The last known state root hash of C_r enables verifying the user's balance of T_{mint} . If
 132 the user had v tokens of T_{mint} on C_r at the point when the last state root was given to the
 133 SC_{oracle} , they can generate a Merkle Tree proof for that and invoke a *Withdraw* transaction
 134 on $SC_{deposit}$. When the proof verification succeeds, v tokens of T_{orig} are transferred from
 135 the $SC_{deposit}$ contract to the user's balance. Every withdrawal transaction is logged in the



■ **Figure 1** The SONIC GATEWAY cross-chain bridge between blockchains C_s and C_r .

136 *withdrawals* array to prevent double withdrawals.

137 Finally, it is possible that the user has deposited and locked some v tokens of T_{orig} on C_s ,
 138 but has not yet claimed them, or they claimed them but there was no state root update after
 139 that claim, so there are no corresponding tokens on T_{mint} that they could retrieve using the
 140 *Withdraw* operation. A *Cancel* transaction must be used in such cases. With this transaction,
 141 the user provides a *Lock* transaction ID (which can be easily checked to exist using the *locks*
 142 log of $SC_{deposit}$ on C_s) and the Merkle tree proof that there was no corresponding *Mint* on
 143 SC_{claim} on C_r in the last known state (verified by checking the *mints* log). Once the *Cancel*
 144 transaction is successful, to prevent double cancellation, the information about the canceled
 145 *Lock* transaction is removed from the *locks* log.

146 3 Specification

147 This section briefly outlines the Isabelle/HOL specification of the Sonic fail-safe bridge. Due
 148 to space constraints, many details are omitted. For full details, we refer the reader to the Isa-
 149 belles/HOL source, available at https://github.com/filipmaric/bridge_formalization.
 150 We expressed the Sonic bridge implementation, originally in Solidity, as a purely functional
 151 program in Isabelle/HOL. Translation from Solidity to Isabelle/HOL is done manually, trying
 152 to be as close as possible to Solidity's semantics. For simplicity, the basic types of Solidity
 153 (`uint256`, `bytes32`, `address`) are all modeled as natural numbers in Isabelle/HOL, ignoring
 154 overflow issues. In Solidity, mappings storing natural numbers default to 0 for non-existent
 155 keys. The function `lookup_nat` (and similarly `lookup_bool`) that we define and use mimics
 156 that behavior. An Isabelle/HOL record models the internal state of each contract.

```
record ERC20State =
  balances :: "(address, uint256) mapping"
  ...
record SCDepositState =
  locks :: "(uint256, bytes32) mapping"
  withdrawals :: "(address, bool) mapping"
  SCOracleAddr :: address
  deadState :: bytes32
  ...
```

157 The `balances` mapping in the `ERC20State` assigns token amounts to user addresses. In
 158 the `SCDepositState`, the `locks` mapping records all successful *Lock* transactions, mapping
 159 transaction IDs to hash values derived from the sender address, token, and amount. The
 160 `withdrawals` mapping tracks users who executed *Withdraw* transactions to retrieve balances

161 from the dead bridge. The address of SC_{oracle} is stored in `SCOracleAddr`, while `deadState`
 162 holds the last valid state root before the bridge failure (0 indicates the bridge is not declared
 163 dead). States of other contracts (e.g., `SCClaimState`) are similarly defined.

164 The storage states of all contracts define the blockchain state, mapping contract addresses
 165 to their respective states. Due to the Isabelle/HOL type system, each smart contract type
 166 requires a separate mapping.

```
record Contracts =
  IERC20 ::      "(address, ERC20State) mapping"
  ISCDeposit ::  "(address, SCDepositState) mapping"
  ISCClaim ::    "(address, SCClaimState) mapping"
  ...
```

167 We define functions to read and modify smart contract states. For example, the following
 168 helper function reads a user's balance from the specified ERC20 contract state.

```
definition balanceOf :: "ERC20State  $\Rightarrow$  address  $\Rightarrow$  uint256" where
  "balanceOf state account = lookup_nat (balances state) account"
```

169 As in Solidity, contract functions can be called on a chain via a contract address. For
 170 instance,

```
definition callBalanceOf :: "Contracts  $\Rightarrow$  address  $\Rightarrow$  address  $\Rightarrow$  Status  $\times$  uint256" where
  "callBalanceOf C address account =
    (case ERC20state C address of
      None  $\Rightarrow$  (Fail "wrong address", 0)
      | Some state  $\Rightarrow$  (Success, balanceOf state account))"
```

171 Each call may fail, e.g., if no valid contract exists at the given address. In such cases, the
 172 chain state remains unchanged. We defined an Isabelle/HOL counterpart for each contract
 173 function by following our Solidity implementation closely. For example, the following Solidity
 174 function in the `SCDeposit` contract checks whether the bridge is dead. The last valid state
 175 root hash is stored in the `deadState` field when the bridge fails.

```
function getDeadStatus() public returns (bool) {
  if (deadState != 0) // we already know that the bridge is dead
    return true;
  // if too much time has passed since the last UPDATE, we declare that
  // the bridge is dead and remember its last known state root hash
  uint256 lastUpdateTime = IStateOracle(stateOracle).lastUpdateTime();
  if (lastUpdateTime != 0 &&
    lastUpdateTime < block.timestamp - TIME_UNTIL_DEAD) {
    deadState = IStateOracle(stateOracle).lastState();
    return true;
  }
  return false;
}
```

176 This function is implemented in Isabelle/HOL as follows:

```
definition getDeadStatus where
  "getDeadStatus C state block =
    (if deadState state  $\neq$  0 then (Success, True, state)
     else let (status, lastUpdateTime) = callLastUpdateTime C (SCOracleAddr state) in
       if status  $\neq$  Success then (status, False, state))"
```

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```

else if lastUpdateTime ≠ 0 ∧
  lastUpdateTime < (timestamp block) - TIME_UNTIL_DEAD then
  let (status, lastState) = callLastState C (SCOracleAddr state) in
  if status ≠ Success then (status, False, state)
  else (Success, True, state (| deadState := lastState |))
else (Success, False, state) )"

```

177 The function returns a triple: the first element indicates success or failure, the second
 178 whether the bridge is dead, and the third the updated state. Monad syntax could remove
 179 explicit state passing and status checks.

180 In our Solidity implementation, some contract functions verify Merkle tree proofs to
 181 confirm the presence of specific memory content in another chain, ensuring a key-value pair
 182 exists in a mapping. Our specification follows a stepwise refinement approach, omitting
 183 proof details and instead postulating axioms that these proofs must satisfy. These axioms
 184 are expressed as Isabelle/HOL [4]. First, we postulate that the following functions can be
 185 defined so that they satisfy the two given axioms:

- 186 ■ `generateStateRoot` creates a state root hash value,
- 187 ■ `generateLockProof` generates a proof for the fact that `lock[ID] = val`,
- 188 ■ `verifyLockProof` verifies if the given proof is valid for the given state root.

```

locale ProofVerifier =
  fixes SCDepositAddress :: "address"
  fixes generateStateRoot :: "Contracts ⇒ bytes32"
  fixes generateLockProof :: "Contracts ⇒ uint256 ⇒ bytes"
  fixes verifyLockProof :: "uint256 ⇒ bytes32 ⇒ bytes32 ⇒ bytes ⇒ bool"
  — if a proof for ID and val verifies, then locks[ID] = val
  assumes verifyLockProofE: "∧ C state ID stateRoot proof val.
    [[SCDepositState C SCDepositAddress = Some state;
      generateStateRoot C = stateRoot;
      verifyLockProof ID val stateRoot proof = True]] ⇒
      getLock state ID = val"
  — if locks[ID] = val, then a proof for ID and val can be generated
  assumes verifyLockProofI: "∧ C ID state stateRoot proof val.
    [[SCDepositState C SCDepositAddress = Some state;
      generateLockProof C ID = proof;
      generateStateRoot C = stateRoot;
      getLock state ID = val]] ⇒
      verifyLockProof ID val stateRoot proof = True"

```

189 We also postulate the honesty assumption for the consensus of users who perform the
 190 regular state root updates, by assuming that whenever an *Update* operation succeeds the
 191 state root hash given to the oracle is indeed the state root hash of the current blockchain
 192 state (as generated by the `generateStateRoot` function).

```

assumes updateSuccess: "∧ C address block blockNum stateRoot C'.
  callUpdate C address block blockNum stateRoot = (Success, C') ⇒
  stateRoot = generateStateRoot C"

```

193 This is sufficient to define the token mint operation and prove its properties (for other
 194 operations, in the same manner we introduce mint proofs, burn proofs, balance proofs etc.).
 195 A concrete implementation for these three abstract functions should be provided at later

196 stages. This implementation can be based on Merkle-tree proofs (as used in our Solidity
 197 implementation), but other types of proofs, such as zero-knowledge proofs, could also be
 198 used. For illustration, we present our specifications for the mint function.

definition mint where

```
"mint C msg state ID token amount proof =
  (if getMint state ID then (Fail "Already claimed", state, C)
   else — verify proof of the deposit on the sender chain
     let hash = hash3 (sender msg) token amount;
     (status, lastState) = callLastState C (SCOracleAddr state) in
     if status ≠ Success then (status, state, C)
     else let status = callVerifyLockProof C ID hash lastState proof in
       if status ≠ Success then (status, state, C)
       else — find the address of the minted token ERC20 contract
         let (status, mintedToken) = callOriginalToMinted C token in
         if status ≠ Success then (status, state, C)
         else if mintedToken = 0 then
           (Fail "No minted token for given token", state, C)
         else — mint the tokens and log the claim
           let state' = setMint state ID True;
           (status, C') = callERC20Mint C mintedToken (sender msg) amount in
           if status ≠ Success then (status, state, C)
           else (Success, state', C'))"
```

199 A blockchain state is considered reachable from a starting state if a sequence of successful
 200 operations (steps, transactions) exists that leads to the final state when executed starting
 201 from the initial state. To define this relation, we first introduce a representation of the steps
 202 (with comments after each step type indicating the step parameters).

datatype Step =

```
LOCK address address uint256 address uint256
— SCDepositAddress caller ID token amount
| MINT address address uint256 address uint256 bytes
— SCCLAIMAddress caller ID token amount proof
...
```

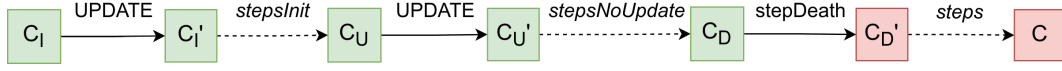
203 Each step is executed by calling its corresponding function on some chain contract.

primrec executeStep ::

```
"Contracts ⇒ nat ⇒ Block ⇒ Step ⇒ Status × Contracts" where
"executeStep C blockNum block (LOCK address caller ID token amount) =
  callLock C address block (message caller amount) ID token amount"
| "executeStep C blockNum block (MINT address caller ID token amount proof) =
  callMint C address (message caller amount) ID token amount proof"
...
```

204 Finally, we inductively define reachability between two blockchain states. Each state is
 205 reachable from itself by the empty list of steps. If C' is reachable from C by a list **steps**,
 206 and executing **step** reaches C'' from C' , then C'' is reachable from C by the list obtained by
 207 joining **steps** and **step**.

```
inductive reachable :: "Contracts ⇒ Contracts ⇒ Step list ⇒ bool" where
  reachable_base: " $\bigwedge C. \text{reachable } C \ C \ []$ "
| reachable_step: " $\bigwedge C \ C' \ \text{blockNum} \ \text{block} \ \text{step}. \llbracket \text{reachable } C \ C' \ \text{steps};$ 
```



■ **Figure 2** General configuration of a dead bridge

$$\text{executeStep } C' \text{ blockNum block step} = (\text{Success}, C'') \parallel \implies \text{reachable } C \ C'' \ (\text{step} \ \# \ \text{steps})"$$

Steps issued by a specific caller are interleaved with steps issued by other users. When distinguishing between them is important, we use the predicate `reachableInterlaved caller C C' stepsCaller stepsOther`, which is also defined inductively. The following function, defined by primitive recursion, checks whether the given list of steps can be successfully executed, regardless of the steps taken by other users.

```

primrec executableSteps :: "address  $\Rightarrow$  Contracts  $\Rightarrow$  Step list  $\Rightarrow$  bool" where
  "executableSteps caller C [] = True"
| "executableSteps caller C (stepCaller # stepsCaller)  $\longleftrightarrow$ 
  executableSteps caller C stepsCaller  $\wedge$ 
  ( $\forall C'$  stepsOther. reachableInterlaved caller C C' stepsCaller stepsOther  $\longrightarrow$ 
  executableStep caller C' stepCaller)"

```

213 4 Correctness proofs

We have proven numerous properties of our bridge, beginning with simple, low-level technical properties and culminating in high-level properties that express user safety. The proof concludes with the central fail-safety theorem, which states that even when the bridge is dead, every user can execute a series of transactions to retrieve all their assets (i.e., the tokens they locked, plus the tokens received from others, minus the tokens transferred to others). Our fail-safety features ensure this guarantee and the primary challenge was to prove it formally. The main idea of the proof is as follows.

- If the bridge is alive, after the deposit by a `LOCK`, the user can make a `MINT`, then a `BURN`, and finally `RELEASE` to retrieve their tokens on the sender chain.
- Assume that the bridge is dead and that the last valid state known on `SCDeposit` is C (that is the state when the last `UPDATE` happened before the bridge became unresponsive).
 - If only the `LOCK` occurred before C , and the tokens have not been claimed (or if `MINT` occurred after the last state update), the user can retrieve their funds using the `CANCEL_WD` operation.
 - If a `MINT` is recorded in C , and there was no `BURN` after it (or if it occurred after the last state update), the user has minted tokens in C , and can retrieve them using the `WITHDRAW_WD` operation.
 - Finally, if a `BURN` is recorded in C , the user can retrieve their tokens using the standard `RELEASE` operation (just as they would while the bridge is active).

Many theorems share assumptions describing the situation where the bridge is dead. Instead of repeating these assumptions in every theorem and deriving their consequences in each proof, we used Isabelle/HOL locales [4]. We defined the locale `BridgeDead` to describe the state of a dead bridge. This situation is depicted in Fig. 2. The execution begins in some initial state C_I . For simplicity, we assume that the first operation after the bridge is deployed is a state `UPDATE`, which transitions it to state C_I' . After this, the bridge operates normally,

executing a sequence of steps denoted by `stepsInit`. At some state $\mathcal{C}_U$, the final state `UPDATE` occurs, leading to state $\mathcal{C}'_U$. Following that, additional steps (denoted by `stepsNoUpdate`) are executed before the bridge becomes inactive. The step that indicates the bridge is dead is denoted by `stepDeath`. At this point, the field `deadState` in the `SCDeposit` contract is set to the state root of the last known valid state, which in this case is $\mathcal{C}_U$. Subsequently, more steps (denoted by `steps`) are executed on the `SCDeposit` contract, leading to the current state $\mathcal{C}$. The complete sequence of all steps from $\mathcal{C}_I$ to $\mathcal{C}$ is denoted by `stepsAll`.

Several auxiliary functions are defined to compute token amounts to formulate the central fail-safety theorem.

- `depositedAmountTo` — this function calculates the total amount of tokens T_{orig} that a caller has deposited into `SCdeposit` by executing `Lock` transactions.
- `retrievedAmountFrom` — this function calculates the total amount of tokens T_{orig} that a caller has retrieved from the contract `SCdeposit` by executing `Release`, `Withdraw`, and `Cancel` transactions.
- `transferredAmountFrom` — this function calculates the total amount of minted tokens T_{mint} on the bridge `SCclaim` that the caller has transferred to other users, while the function `transferredAmountTo` calculates the total amount of T_{mint} that other users have transferred to the caller.

When the bridge dies, `SCoracle` contains a state root that encodes aggregated information about all transactions that occurred before the last update before the bridge's failure (i.e., transactions in the list `stepsInit` in Figure 2). After this update, transactions (including mints, burns, and transfers) are ignored. We consider a user to have retrieved all their assets if the total amount of tokens they invested (defined as the sum of T_{orig} they locked up to the current state and the T_{mint} they transferred to other users before the last update) is equal to the total amount of tokens they gained (defined as the sum of T_{orig} they retrieved via a `Release`, `Withdraw`, or `Cancel` transaction and the T_{mint} they received from other users before the last update).

definition `allTokensRetrieved` where

```
"allTokensRetrieved SCDepositAddr SCclaimAddr token caller stepsAll stepsInit ≡
  retrievedAmountFrom SCDepositAddr token caller stepsAll +
  transferredAmountFrom SCclaimAddr token caller stepsInit =
  depositedAmountTo SCDepositAddr token caller stepsAll +
  transferredAmountTo SCclaimAddr token caller stepsInit"
```

Our central theorem demonstrates that, from any state $\mathcal{C}$ in which the bridge is dead, each user can issue a list of transactions that will be executable regardless of the transactions made by other users. Moreover, executing these transactions will always result in a state where the user has retrieved all of their tokens.

theorem `paybackPossibleBridgeDead`:

```
shows "∃ steps.
  (∀ step ∈ set steps. isCaller caller step) ∧
  executableSteps caller C steps ∧
  (∀ C' stepsOther. reachableInterleaved caller C C' steps stepsOther →
    allTokensRetrieved token caller
      ((interleaveSteps steps stepsOther) @ stepsAll) stepsInit)"
```

The steps in the list `stepsAll` lead from $\mathcal{C}_{init}$ to $\mathcal{C}$. The steps `interleaveSteps steps stepsOther`, obtained by interleaving the unpredictable steps of other users `stepsOther`

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with the steps `steps` issued by the current user, lead from $\mathcal{C}$ to $\mathcal{C}'$, where all tokens have been successfully retrieved.

Note that a similar, less interesting theorem can be proven when the bridge is not dead (under some additional assumptions on the frequency of updates). In this scenario, the caller only needs to issue `MINT`, `BURN`, and `RELEASE` transactions. However, there is no guarantee that the bridge will not fail during the execution of these transactions. If this occurs, the user must switch to the recovery strategy used when the bridge is dead.

Many necessary lemmas contribute to the proof of the central theorem. We formulated and proved lemmas that ensure the executability of each specific operation. For instance, the following theorem guarantees lock cancellation is possible if no claim of minted tokens was made before the last update before the bridge became inactive and if no cancellation occurred before the current state.

```
lemma cancelPossible:
  assumes "LOCK SCDepositAddr caller ID token amount ∈ set stepsAll"
  assumes "¬ isMintedID SCClaimAddr token ID stepsInit"
  assumes "¬ isCanceledID SCDepositAddr token ID stepsAll"
  assumes "proof = generateClaimProof CU ID"
  shows "let step = CANCEL_WD SCDepositAddr caller ID token amount proof
        in fst (executeStep C block blockNum step) = Success"
```

Theorems for other "rescue" operations are similar. It is typically necessary to prove that a particular step is possible by showing that some data is set in the required manner. For example, canceling a deposit ID by a caller who requests a specific token amount is only possible if the proof that guarantees that `locks[ID] = hash(caller, token, amount)` can be verified. It is proved (by induction) that this data guarantees that there was a prior `LOCK` operation from the `caller` for the given `amount` of the give `token` T_{orig} (assuming that hash function is injective, which is a widespread assumption in a blockchain setting). However, repaying tokens for a canceled deposit also requires enough tokens T_{orig} in the `SCDeposit` contract balance. This is the most challenging part of the entire proof, as it requires careful analysis of the "cash flow" across all parts of the bridge, considering all operations and steps. Such invariants are proven both globally (characterizing the `SCDeposit` contract balance after transactions from all users) and on a per-user basis (characterizing T_{orig} and T_{mint} balances for each user). Due to space constraints, we will describe only the former. We introduce the following quantities (all are natural numbers, so they are non-negative):

- `SCDepositBalance` – the current token balance of the given $SC_{Deposit}$ address.
- `locked / canceled / withdrawn / released` – the total sum of amounts in all `LOCK / CANCEL_WD / WITHDRAW_WD / RELEASE` steps for a given $SC_{deposit}/SC_{claim}$ address and token.
- `mintedBeforeDeath` – the total sum of amounts in all `MINT` steps executed before the last update before the bridge becomes inactive.
- `nonMintedBeforeDeath` – the total sum of amounts in all `LOCK` steps whose ID is not claimed (minted) before the last update before the bridge becomes inactive.
- `nonCanceledNonMintedBeforeDeath` – the total sum of amounts in all `LOCK` steps whose ID is not minted before the last update before the bridge becomes inactive and which has not been canceled.
- `nonWithdrawnNonBurnedMintedBeforeDeath` – the total amount of tokens produced by `MINT` steps that have not been burned before the last update before the bridge becomes inactive, and have not been withdrawn.

- 312 ■ `burnedBeforeDeath` – the total sum of amounts in `BURN` steps for a given address and
313 token that were executed before the last update, when the bridge becomes inactive.
- 314 ■ `nonReleasedBurnedBeforeDeath` – the total sum of amounts in all `BURN` steps for a given
315 address and token, that were executed before the last update before the bridge becomes
316 inactive whose ID has not yet been released.

317 Then, we proved the following five invariants.

- 318 1. `locked = SCDepositBalance + canceled + withdrawn + released`
- 319 2. `locked = mintedBeforeDeath + nonMintedBeforeDeath`
- 320 3. `nonMintedBeforeDeath = canceled + nonCanceledNonMintedBeforeDeath`
- 321 4. `mintedBeforeDeath = withdrawn + nonWithdrawnNonBurnedMintedBeforeDeath +`
322 `burnedBeforeDeath`
- 323 5. `burnedBeforeDeath = released + nonReleasedBurnedBeforeDeath`

324 The first invariant is proved by induction by analyzing the transactions that change the
325 token deposit balance. The second invariant is trivial. The others focus on specific operations
326 and are proven by induction and case analysis of the last applied step, where most steps
327 are irrelevant (for example, only `MINT` and `CANCEL_WD` operations are relevant for the third
328 invariant). Combining these four invariants yields

$$\begin{aligned} 329 \quad & \text{SCDepositBalance} = \text{nonCanceledNonMintedBeforeDeath} + \\ 330 \quad & \text{nonWithdrawnNonBurnedMintedBeforeDeath} + \text{nonReleasedBurnedBeforeDeath} \end{aligned}$$

331 From this, we can guarantee sufficient funds for each rescue operation. For instance, when
332 proving that a cancel step is possible, there is a deposit that was not claimed before the last
333 update before the bridge died and that has not yet been canceled. Therefore, the it's amount
334 is included in the `nonCanceledNonMintedBeforeDeath` quantity, which, by the previous
335 invariant, is less than or equal to the `SCDepositBalance`, i.e., the current token balance of
336 the `SCDeposit` contract. Since the amount the caller requires must match the amount they
337 deposited (which we know from the value of `locks[ID] = hash(caller, token, amount)`,
338 and the assumed injectivity of the `hash` function), the contract contains the required tokens,
339 making the payback possible. Similar reasoning applies to all other operations.

340 Many other lower-level properties had to be proven to support the correctness proof. For
341 example, each *Mint* must be preceded by a *Lock*, only the entity who made a lock can mint
342 the tokens, once the bridge dies, it can never become life again, etc. We refer readers to the
343 Isabelle/HOL proof documents for their formalization.

344 5 Evaluation and Discussion

345 The Isabelle formalization was completed by a single individual who had worked part-
346 time on this project for over six months. A rough estimate suggests the formalization
347 required approximately 2–3 full person-months of effort. Isabelle's definition of the bridge's
348 formal model comprises around 900 lines of code (LOC), including approximately 50 defined
349 functions, while the accompanying proofs span roughly 15,000 LOC. The current proof
350 contains approximately 750 lemmas and theorems. The proof-checking process takes around
351 8 minutes on a standard laptop computer (Intel(R) Core(TM) i5-8265U CPU @ 1.60GHz,
352 8GB of RAM). However, this time could be significantly reduced by replacing several
353 time-consuming, fully automated proofs with more detailed manual proofs.

354 Several underlying assumptions in our model pose threats to validity and must be
355 addressed to ensure the total correctness of a real-world bridge implementation. Some of
356 these assumptions can be easily ensured through a correct deployment process.

5:12 Formal Verification of a Fail-Safe Cross-Chain Bridge

- 357 ■ It is assumed that contracts are correctly deployed and initialized, i.e., that all addresses
358 are correctly set up.
 - 359 ■ It is assumed that each bridge and original token has a dedicated minted token, i.e., that
360 minted tokens are not shared.
 - 361 ■ It is assumed that users initially have no minted tokens after the bridge is deployed.
 - 362 ■ It is assumed that an `UPDATE` operation occurs immediately after the bridge is deployed,
363 i.e., that the bridge never operates in a state where state roots are uninitialized.
- 364 Other assumptions include the following:
- 365 ■ It is assumed that arithmetic overflows will not occur while the bridge is in operation.
366 This is reasonable, as the only arithmetic operations involve updating user token balances.
 - 367 ■ It is assumed that the hash function is injective (i.e., no hash collisions) and always
368 produces a nonzero value. This is a common assumption underlying blockchain security.
 - 369 ■ It is assumed that (Merkle-tree) proof checking is fully sound. This is also reasonable, as
370 the correctness of Merkle trees has been formally verified.
 - 371 ■ Transaction fees and gas prices are not included in our model.
 - 372 ■ Reentrancy attacks are not considered. Although reentrancy poses a significant threat in
373 Solidity smart contracts, it can be prevented through careful implementation (e.g., by
374 following the checks-effects-interactions pattern).
 - 375 ■ It is assumed that updates are reliable, i.e., that validators are always honest. This
376 assumption may be the most problematic, as many successful bridge attacks have been
377 carried out by corrupting validators [35]. While specifying the details of a validation
378 protocol can help relax this assumption, some risks will always remain. For example,
379 private keys must be kept secure.

380 6 Related Work

381 BFT consensus protocols have been verified using interactive theorem provers. The work in [7]
382 develops a modular proof in TLA+ for DAG-based consensus protocols. The work in [27]
383 uses the IVy interactive theorem prover [1] to formally verify a variant of the Moonshine
384 consensus protocol [27]. The work in [22] uses IVy and Isabelle/HOL [25] to verify the
385 Stellar Consensus Protocol [21]. The Algorand [14] consensus protocol has been verified using
386 Coq [13]. The safety of several non-Byzantine protocols, such as variants of Paxos [11, 29]
387 has been verified using interactive theorem proving. To the best of our knowledge, we are
388 the first to propose formal proof for a cross-chain bridge, particularly bridge failure safety.

389 There has been foundational work in the verification of Ethereum smart contracts. These
390 contracts are compiled into Ethereum Virtual Machine (EVM) bytecode, formally defined for
391 use with interactive theorem provers [15]. A sound program logic at the bytecode level has
392 also been developed [3]. Typically, smart contracts are written in the Solidity programming
393 language, with formal semantics defined in Isabelle/HOL [23]. Another proposed approach in
394 smart contract verification is to define them in specialized languages converted to low-level
395 byte code using verified compilers. For example, Britten's PhD thesis [9] explores techniques
396 to improve the reliability and security of smart contracts by leveraging formal verification
397 methods through interactive theorem proving in Coq, combined with a verified compiler from
398 the language DeepSEA [31]. In [28], Ribeiro defines the imperative language SOLI within
399 Isabelle/HOL that captures a significant subset of Solidity, and develops big-step, Hoare logic,
400 and a proof system for it, with soundness and completeness results formally established.

Our approach differs in that the formal bridge model is currently represented as a functional program within Isabelle/HOL, derived through manual translation from Solidity. Consequently, our current work establishes only the correctness of a high-level bridge model, leaving the verification of its Solidity implementation for future work.

Various automated tools analyze Solidity code and detect bugs or violations of specific safety properties (for example, since 2019, the Solidity compiler has included a model checker, SolMC [2]). However, a key limitation of these tools is their lack of effectiveness in expressing and verifying liquidity properties. Some automated tools are also designed explicitly for verifying liquidity properties, such as Solvent [5].

Our decision to use the interactive theorem prover Isabelle/HOL instead of automated tools was influenced by our prior experience and the fact that any limitations in automated prover support can be overcome by reverting to manual proofs. One possible research direction would be to examine whether state-of-the-art automated tools are capable of proving the liquidity properties of large-scale projects such as a crypto-bridge.

7 Conclusion

This paper describes the SONIC GATEWAY fail-safe bridge design and its formalization in Isabelle/HOL. We have formally proven that users can still retrieve all their assets on the sender chain even if the bridge becomes unresponsive on the receiver chain.

Our current abstract model does not account for numerous essential real-world issues, such as gas consumption, potential overflows, reentrancy vulnerabilities, and other Solidity-specific implementation challenges. Addressing these practical concerns will be an integral part of our efforts to ensure that the model reflects these complexities and security requirements in a real-world deployment. Therefore, we plan to bridge the gap between the current abstract Isabelle/HOL bridge model and its real Solidity implementation in our future work. To achieve this, we must provide a detailed description of the Inter-Blockchain Communication (IBC) Relay, which utilizes Merkle-tree proofs and whose correctness is currently only assumed in our formalization. Additionally, we plan to leverage the formal semantics of Solidity in Isabelle/HOL [23] to verify our bridge up to the Solidity implementation level fully formally.

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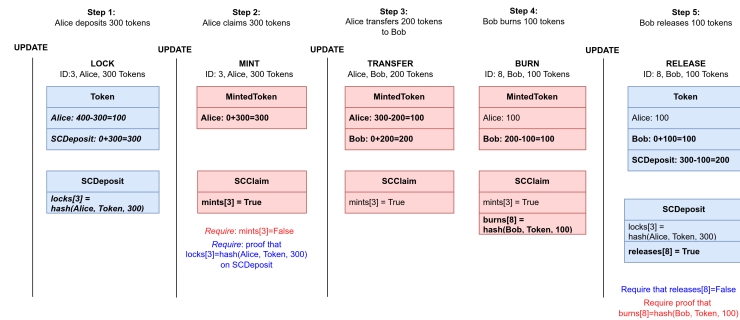


Figure 3 Example of lock/mint, burn/release operations. Sender blockchain contracts are depicted in blue, and receiver contracts in red.

A Detailed Bridge Example

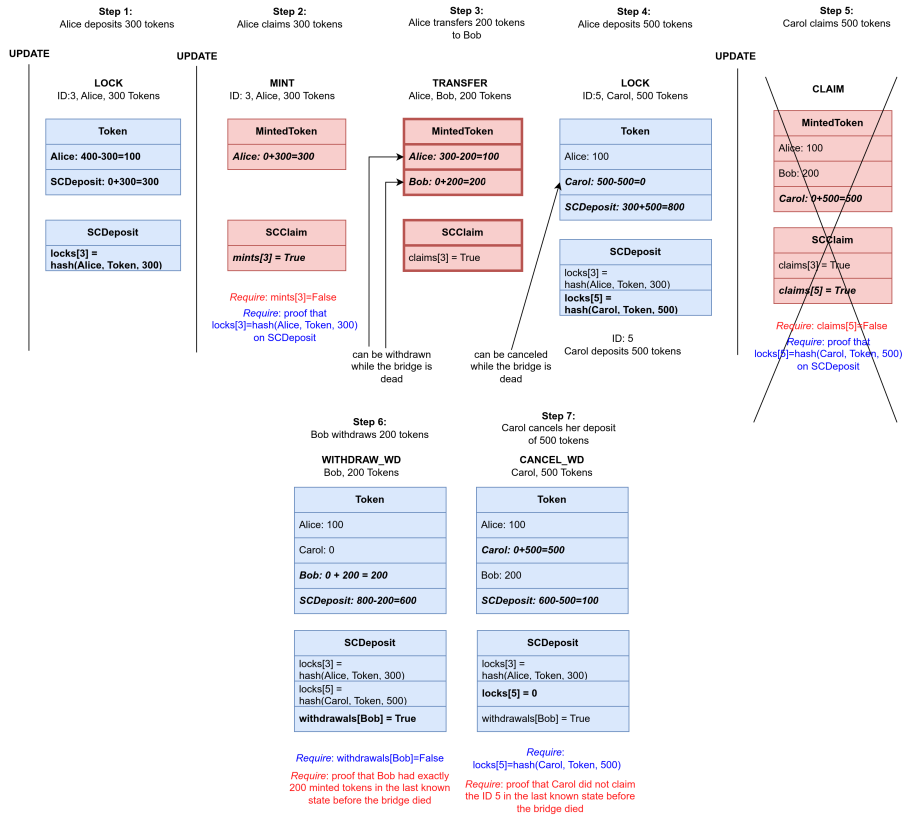
An example showing basic bridge operations is shown in Figure 3. Bridge operations are supported by two smart contracts on the sender chain (our custom contract *SCDeposit* and an ERC20 contract *Token*), and two smart contracts on the receiver chain (our custom contract *SCClaim* and an ERC20 contract *MintedToken*).

We assume that Alice has 400 tokens on the sender chain and she wants to transfer 300 tokens to the receiver chain. She invokes a **LOCK** operation on the *SCDeposit* contract on the sender chain, that transfers 300 tokens from her balance to the *SCDeposit* contract balance. Information about this transaction is logged in the *SCDeposit* contract, in a special **locks** mapping, by assigning a hash value that combines information about the caller (Alice, i.e., her unique address), the currency (Token, i.e., its unique address), and the amount (300) to the unique transaction ID (it is 3, in this example). This information is later used to confirm that this transaction occurred.

In the next step, Alice invokes a **MINT** transaction on the *SCClaim* contract on the receiver chain. If that transaction succeeds, 300 tokens will be added to her balance on the *MintedToken* contract („minted out of thin air”). However, for this to be possible, (1) these 300 tokens should be justified by the 300 tokens deposited on the sender chain, and (2) it should be ensured that she can do this only once. For this, it is assumed that she sends the ID of the original **LOCK** transaction (the value 3) as a parameter of this claim. Requirement (2) is easily ensured by maintaining a special **mints** mapping in the *SCClaim* contract. Before the claim, the value **mints**[ID] must be False, and is set to True once the minting is done. Requirement (1) is harder to achieve, because it requires information about the data stored in the sender chain. From the value assigned to the key ID in the **locks** log of the *SCDeposit* contract, we can check that Alice was the one who deposited 300 tokens (assuming that there are no hash collisions, which is a rather common assumption). To be able to do this, we rely on Merkle-tree proofs and consensus on the root hash of the sender chain. During regular updates, a consensus of trusted verifiers agrees on the root hash value and writes it to a special place (for this, a special *StateOracle* contract is used). When Alice wants to claim the minted tokens, she provides a Merkle tree proof for the value assigned to **locks**[ID]. The *Bridge* contract then verifies if this value is equal to the hash value that combines her address, the token address, and the deposited amount, and if it is, the transaction succeeds.

Next, we assume that Alice transfers 200 minted to Bob. It is a regular ERC20 transfer operation, and no additional checks and loggings are performed.

Next, we assume that Bob wants to transfer 100 of these minted tokens back to the



■ **Figure 4** Example of the fail-safe mechanism used if the bridge dies (becomes unresponsive).

581 sender chain. For this, he must first burn the tokens on the receiver chain. He invokes a
582 **BURN** operation which reduces his balance (minted tokens are “burned and destroyed”), and
583 then logs this information by assigning the hash that combines the information about the
584 caller (Bob), the currency (Token) and the amount (100) to the unique transaction ID (it is
585 8 in this example) in a special **burns** mapping in the *SCClaim* contract.

586 Finally, Bob releases 100 tokens on the sender chain, by transferring them from the
587 *SCDeposit* balance in the *Token* contract to his balance. Again, it must be ensured that (1)
588 these are covered by the burned 100 tokens on the bridge, and that (2) this release is done
589 exactly once. Requirement (2) is easily ensured by using a special **releases** mapping in
590 the *SCDeposit* contract (the value True is assigned to the unique transaction ID once the
591 release is done). To ensure (1), we again use Merkle-tree proofs and the state root set by the
592 consensus of verifiers in the **UPDATE** operation (this time sender chain must be informed about
593 the state root of the receiver chain at certain block height). Bob must supply a Merkle-proof
594 that the value **burns**[ID] is equal to the hash value of the caller (Bob), the currency (Token)
595 and the amount 100. If the Merkle-tree proof verification succeeds, we know that Bob really
596 burned his 100 tokens on the receiver chain, so we can transfer him the required 100 tokens.

597 Our bridge has a fail-safety mechanism that enables users to retrieve their funds on
598 the sender chain, even when the contracts on the receiver chain become unresponsive. An
599 example of this feature in operation is shown in Fig. 4.

600 We assume that the first three steps are the same as in the previous example. Next, we
601 assume that Carol makes a deposit and locks 500 tokens on the sender chain, and that after
602 that she makes a successful claim and mints those 500 tokens on the receiver chain. For

603 this to succeed, there must have been an `UPDATE` step in between in which the *StateOracle*
 604 contract has been informed about the state roots of the chains. Just after the `MINT` step, the
 605 bridge dies and becomes unresponsive. If someone tries to release the funds on the sender
 606 chain, he would be able to do this only if the burned them prior to that last `UPDATE` (since,
 607 the effect of those `BURN` operations is encoded in the current state root). However, users
 608 that have funds on the failed receiver bridge that have not been burned before that update,
 609 cannot retrieve them. The operations that happened after that last `UPDATE` step are not
 610 visible from the sender chain, so it is assumed that the state of the receiver chain in the
 611 moment of that last `UPDATE` step is its *last valid state*, also called the *dead state* (it is the
 612 state after the step 3 in Fig. 4). After some predetermined time period in which there are no
 613 new updates, the sender chain realizes that the bridge is dead and switches to fail-safe mode.
 614 This is irreversible, since, even if the bridge becomes operational again, the contract on the
 615 sender chain will not take that into account. In the fail-safe mode, all users who had minted
 616 tokens in the last valid state can withdraw them as original tokens on the sender chain.

617 We assume that Bob wants to withdraw his 200 tokens that he got from Alice, so he
 618 invokes a special withdraw while dead (`WITHDRAW_WD`) operation. He can do this only once,
 619 and for this, he must provide a Merkle-tree proof that he had exactly 200 minted tokens
 620 in the last valid state. If this proof successfully verifies, he is given his 200 tokens from the
 621 *TokenDeposit* contract balance, and this is logged in a special `withdrawals` mapping (the
 622 value `withdrawals[Bob]` is set to `True`, guaranteeing that Bob has withdrawn all his funds
 623 and will not be able to do this again.

624 However, there is a problem with Carol. She has made a successful claim while the bridge
 625 was alive, but the bridge died before another `UPDATE` step, so from the sender chain, it is
 626 not visible that she has some minted tokens, and she cannot invoke `WITHDRAW_WD` operation
 627 to retrieve her funds. However, since the last valid state was prior to her claim, it is also
 628 not visible from the sender chain. Therefore, she has the same status as the users that have
 629 made a deposit, but did not claim them before the bridge died. They do not have minted
 630 tokens, and cannot withdraw them by proving their balance in the last valid state. Therefore
 631 another special operation is introduced.

632 We assume that Carol invokes the special cancel deposit while dead (`CANCEL_WD`) operation.
 633 She can do this only once and she must provide the unique ID of the original transaction (in
 634 this example, `ID=5`) along with the proof that she has not claimed the funds before the last
 635 valid state (i.e., that `mints[ID]=False` in the last valid state). The hash value assigned to
 636 `locks[5]` in the *SCDeposit* contract verifies that Carol was the one that really deposited
 637 500 tokens. If these two verifications succeed, the deposit is canceled, she is given back
 638 500 tokens, and it is recorded that the deposit with the `ID=5` has been canceled (by setting
 639 `locks[5]=0`, and assuming that 0 cannot be a valid hash value), so Carol cannot repeat this
 640 operation more than once.